AP Statistics Exploration When Does Blocking Help?

A set of 24 dogs (6 of each of 4 breeds, each attending 1 of 4 veterinary clinics) has been randomly selected from a population of dogs older than 8 years of age whose owners have given consent for their inclusion in a study. The purpose of the study is to determine (i) whether there are different changes in bone density over the year of the study for dogs in three treatment groups; and, if so (ii) how much each treatment influences that change in bone density.

Each dog will be assigned to exactly one of three treatments. Group "Ca" will receive a dietary supplement of calcium, Group "Ex" will receive a dietary supplement of calcium and a daily exercise regimen, and Group "Co" will be a control group that receives no supplement to their ordinary diet and no additional exercise. All dogs will be given a bone density evaluation at the beginning and end of the one-year study. Bone density is measured in Houndsfield units--positive values indicate an increase in bone density and negative values represent a decrease.

The Simulation:

We will simulate three possible design scenarios for this study -- Completely Randomized Design, Blocked by Breed, and Blocked by Clinic. Throughout the course of the simulation, YOU will be playing a particular dog who will be assigned to a treatment. Your breed and clinic will not change as we switch designs. However, your treatment may change. Your job is to calculate your change in bone density as a response to your given treatment under each design. My job is to act as the Researcher and randomly assign treatments under each design.

Select your Dog:

You will be dealt a card indicating your dog's name, breed, clinic, and typical dog bone density change. Record that information below. Do not reveal your information to any other dogs.

Name	Breed	Clinic	Dog Density Change

Select a Blue card corresponding to your dog's breed. Note the typical bone density change by breed below.

Select a Yellow card corresponding to your dog's clinic. Note the typical bone density change by clinic below.

Select an Orange card representing "other" contributing factors to bone density. Follow the instructions on the card and record the bone density change below:

Breed Density Change	Clinic Density Change	Other Density Change

Design I: Completely Randomized Design:

One way to assign treatments is to randomly allocate the dogs into three treatment groups. Sketch a completely randomized design for this study below:

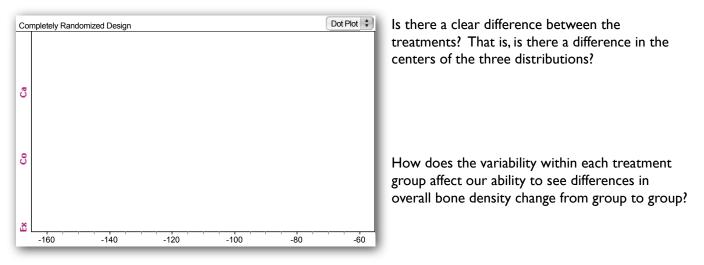
You will be dealt a card indicating your year-long treatment. Record the bone density change from your randomly assigned treatment.

Treatment Density Change

Your total bone density change is based on a combination of your typical dog density change, breed, clinic, other contributing factors, and treatment. Calculate your total bone density change for the completely randomized year-long study and record it below.

Dog	Breed	Clinic	Other	Treatment	TOTAL

There are three stacked dotplots on the board, one for each treatment. Record your total bone density change on the appropriate dotplot and sketch all three below:



Return your Treatment card to the Researcher to prepare for the next simulation.

Design 2: Randomized Block Design, Blocked by Breed:

Another way to assign treatments is to separate the dogs by breed and then randomly allocate the dogs in each breed into three treatment groups.

Sketch a blocked by breed design for this study below:

You will be dealt a card indicating your year-long treatment. Record the bone density change from your randomly assigned treatment.

Treatment Density Change

Your total bone density change is based on a combination of your typical dog density change, breed, clinic, other contributing factors, and treatment. Calculate your total bone density change for the blocked by breed year-long study and record it below.

Dog	Breed	Clinic	Other	Treatment	TOTAL

Locate the other 5 dogs from your breed. Record each dog's bone density change based on treatment below. Then, calculate the overall average bone density change for your breed.

Finally, calculate the effect of the treatment on the average bone density change by subtracting the breed average from each dog's observed response. Why do we do this?

	Observed	Changes			Observed	I-Average
Exercise			Breed Average	Exercise		
Calcium				Calcium		
Control				Control		

There are three stacked dotplots on the board, one for each treatment. Record your "Observed-Average" differences on the appropriate dotplots and sketch all three below:

Blo	cked by Breed	Dot Plot 💲
ő		
8		
Ex	-15 -10 -5 0 5 10	15 20

Is there a clear difference between the treatments? That is, is there a difference in the centers of the three distributions?

Can you estimate the average amounts by which the treatments improve bone density?

Return your Treatment card to the Researcher to prepare for the next simulation.

Design 3: Randomized Block Design, Blocked by Clinic:

Another way to assign treatments is to separate the dogs by clinic and then randomly allocate the dogs from each clinic into three treatment groups.

Sketch a blocked by clinic design for this study below:

You will be dealt a card indicating your year-long treatment. Record the bone density change from your randomly assigned treatment.

|--|

Your total bone density change is based on a combination of your typical dog density change, breed, clinic, other contributing factors, and treatment. Calculate your total bone density change for the blocked by clinic year-long study and record it below.

Dog	Breed	Clinic	Other	Treatment	TOTAL

Locate the other 5 dogs from your clinic. Record each dog's bone density change based on treatment below. Then, calculate the overall average bone density change for your clinic.

Finally, calculate the effect of the treatment on the average bone density change by subtracting the clinic average from each dog's observed response.

	Observed Changes			Observed-Average
Exercise		Clinic Average	Exercise	
Calcium			Calcium	
Control			Control	

There are three stacked dotplots on the board, one for each treatment. Record your "Observed-Average" differences on the appropriate dotplots and sketch all three below:

Blo	cked by Clinic	Dot Plot
Ca		
8		
Ĕ	-15 -10 -5 0 5 10 1	5 20

Is there a clear difference between the treatments? That is, is there a difference in the centers of the three distributions?

In which simulation/design was it easiest to discern the effects of the three treatments?

How did the characteristics of the variables and the design of the allocation work together to make that particular design scheme work best?

You are "Elmer"	You are "Bernie"	You are "Queenie"
Breed: Akita	Breed: Akita	Breed: Akita
Clinic: Treehouse	Clinic: Barking Lot	Clinic: Pooch Palace
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Sugar"	You are "Jock"	You are "Curly"
Breed: Akita	Breed: Akita	Breed: Akita
Clinic: Paw Prince	Clinic: Pooch Palace	Clinic: Treehouse
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Rocky"	You are "Happy"	You are "Nico"
Breed: Beagle	Breed: Beagle	Breed: Beagle
Clinic: Paw Prince	Clinic: Pooch Palace	Clinic: Barking Lot
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Alex"	You are "Pepper"	You are "Snickers"
Breed: Beagle	Breed: Beagle	Breed: Beagle
Clinic: Treehouse	Clinic: Paw Prince	Clinic: Paw Prince
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Buster"	You are "Newton"	You are "Sparky"
Breed: Collie	Breed: Collie	Breed: Collie
Clinic: Barking Lot	Clinic: Pooch Palace	Clinic: Treehouse
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Lad"	You are "Julius"	You are "Cinnamon"
Breed: Collie	Breed: Collie	Breed: Collie
Clinic: Treehouse	Clinic: Paw Prince	Clinic: Barking Lot
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Rex"	You are "Euclid"	You are "Spot"
Breed: Dalmation	Breed: Dalmation	Breed: Dalmation
Clinic: Pooch Palace	Clinic: Pooch Palace	Clinic: Barking Lot
Your Annual Bone	Your Annual Bone	Your Annual Bone
Density Change: -105	Density Change: -105	Density Change: -105
You are "Archie"	You are "Euler"	You are "Lucv"
Breed: Dalmation	Breed: Dalmation	Breed: Dalmation
	Clinic: Paw Prince	Clinic: Treehouse
Your Annual Bone	Your Annual Bone	Your Annual Bone
You are "Archie" Breed: Dalmation Clinic: Barking Lot	You are "Euler" Breed: Dalmation Clinic: Paw Prince	You are "Lucy" Breed: Dalmation Clinic: Treehouse

Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)
Annual Bone Density Change	Annual Bone Density Change	Annual Bone Density Change
Due to Other Sources	Due to Other Sources	Due to Other Sources
MATH: PRB:	MATH: PRB:	MATH: PRB:
RandNormal(0,2)	RandNormal(0,2)	RandNormal(0,2)

Breed: Akita	Breed: Akita	Breed: Akita
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: -2	Change for your Breed: -2	Change for your Breed: -2
Breed: Akita	Breed: Akita	Breed: Akita
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: -2	Change for your Breed: -2	Change for your Breed: -2
Breed: Beagle	Breed: Beagle	Breed: Beagle
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: 9	Change for your Breed: 9	Change for your Breed: 9
Breed: Beagle	Breed: Beagle	Breed: Beagle
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: 9	Change for your Breed: 9	Change for your Breed: 9
Breed: Collie	Breed: Collie	Breed: Collie
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: 32	Change for your Breed: 32	Change for your Breed: 32
Breed: Collie	Breed: Collie	Breed: Collie
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: 32	Change for your Breed: 32	Change for your Breed: 32
Breed: Dalmation	Breed: Dalmation	Breed: Dalmation
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: -39	Change for your Breed: -39	Change for your Breed: -39
Breed: Dalmation	Breed: Dalmation	Breed: Dalmation
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Breed: -39	Change for your Breed: -39	Change for your Breed: -39

Clinic: Treehouse	Clinic: Treehouse	Clinic: Treehouse
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: I	Change for your Clinic: I	Change for your Clinic: I
Clinic: Treehouse	Clinic: Treehouse	Clinic: Treehouse
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: I	Change for your Clinic: I	Change for your Clinic: I
Clinic: Barking Lot	Clinic: Barking Lot	Clinic: Barking Lot
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: 2	Change for your Clinic: 2	Change for your Clinic: 2
Clinic: Barking Lot	Clinic: Barking Lot	Clinic: Barking Lot
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: 2	Change for your Clinic: 2	Change for your Clinic: 2
Clinic: Pooch Palace	Clinic: Pooch Palace	Clinic: Pooch Palace
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: 0	Change for your Clinic: 0	Change for your Clinic: 0
Clinic: Pooch Palace	Clinic: Pooch Palace	Clinic: Pooch Palace
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: 0	Change for your Clinic: 0	Change for your Clinic: 0
Clinic: Paw Prince	Clinic: Paw Prince	Clinic: Paw Prince
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: -3	Change for your Clinic: -3	Change for your Clinic: -3
Clinic: Paw Prince	Clinic: Paw Prince	Clinic: Paw Prince
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change for your Clinic: -3	Change for your Clinic: -3	Change for your Clinic: -3

Treatment:	Treatment:	Treatment:
Control	Control	Control
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
-8	-8	-8
Treatment:	Treatment:	Treatment:
Control	Control	Control
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
-8	-8	-8
Treatment:	Treatment:	Treatment:
Control	Control	Calcium
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
-8	-8	2
Treatment:	Treatment:	Treatment:
Calcium	Calcium	Calcium
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
2	2	2
Treatment:	Treatment:	Treatment:
Calcium	Calcium	Calcium
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
2	2	2
Treatment:	Treatment:	Treatment:
Calcium	Exercise	Exercise
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
2	6	6
Treatment:	Treatment:	Treatment:
Exercise	Exercise	Exercise
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
6	6	6
Treatment:	Treatment:	Treatment:
Exercise	Exercise	Exercise
Annual Bone Density	Annual Bone Density	Annual Bone Density
Change Due to Treatment	Change Due to Treatment	Change Due to Treatment
6	6	6